

# 1

## Introduction

### ANSWERS TO MULTIPLE CHOICE QUESTIONS

- Using a calculator to multiply the length by the width gives a raw answer of  $6783 \text{ m}^2$ , but this answer must be rounded to contain the same number of significant figures as the least accurate factor in the product. The least accurate factor is the length, which contains either 2 or 3 significant figures, depending on whether the trailing zero is significant or is being used only to locate the decimal point. Assuming the length contains 3 significant figures, answer (c) correctly expresses the area as  $6.78 \times 10^3 \text{ m}^2$ . However, if the length contains only 2 significant figures, answer (d) gives the correct result as  $6.8 \times 10^3 \text{ m}^2$ .
- Both answers (d) and (e) could be physically meaningful. Answers (a), (b), and (c) must be meaningless since quantities can be added or subtracted only if they have the same dimensions.
- According to Newton's second law,  $Force = mass \times acceleration$ . Thus, the units of  $Force$  must be the product of the units of  $mass$  (kg) and the units of  $acceleration$  ( $\text{m/s}^2$ ). This yields  $\text{kg} \cdot \text{m/s}^2$ , which is answer (a).
- The calculator gives an answer of 57.573 for the sum of the 4 given numbers. However, this sum must be rounded to 58 as given in answer (d) so the number of decimal places in the result is the same (zero) as the number of decimal places in the integer 15 (the term in the sum containing the smallest number of decimal places).
- The required conversion is given by:

$$h = (2.00 \text{ m}) \left( \frac{1000 \text{ mm}}{1.00 \text{ m}} \right) \left( \frac{1.00 \text{ cubitus}}{445 \text{ mm}} \right) = 4.49 \text{ cubiti}$$

This result corresponds to answer (c).

- The given area ( $1420 \text{ ft}^2$ ) contains 3 significant figures, assuming that the trailing zero is used only to locate the decimal point. The conversion of this value to square meters is given by:

$$A = (1.42 \times 10^3 \text{ ft}^2) \left( \frac{1.00 \text{ m}}{3.281 \text{ ft}} \right)^2 = 1.32 \times 10^2 \text{ m}^2 = 132 \text{ m}^2$$

Note that the result contains 3 significant figures, the same as the number of significant figures in the least accurate factor used in the calculation. This result matches answer (b).

- You cannot add, subtract, or equate a number apples and a number of days. Thus, the answer is yes for (a), (c), and (e). However, you can multiply or divide a number of apples and a number of days. For example, you might divide the number of apples by a number of days to find the number of apples you could eat per day. In summary, the answers are (a) yes, (b) no, (c) yes, (d) no, and (e) yes.

8. The given Cartesian coordinates are  $x = -5.00$ , and  $y = 12.00$ , with the least accurate containing 3 significant figures. Note that the specified point (with  $x < 0$  and  $y > 0$ ) is in the second quadrant. The conversion to polar coordinates is then given by:

$$r = \sqrt{x^2 + y^2} = \sqrt{(-5.00)^2 + (12.00)^2} = 13.0$$

$$\tan \theta = \frac{y}{x} = \frac{12.00}{-5.00} = -2.40 \quad \text{and} \quad \theta = \tan^{-1}(-2.40) = -67.3^\circ + 180^\circ = 113^\circ$$

Note that  $180^\circ$  was added in the last step to yield a second quadrant angle. The correct answer is therefore (b) (13.0,  $113^\circ$ ).

9. Doing dimensional analysis on the first 4 given choices yields:

$$(a) \quad \frac{[v]}{[t^2]} = \frac{L/T}{T^2} = \frac{L}{T^3}$$

$$(b) \quad \frac{[v]}{[x^2]} = \frac{L/T}{L^2} = L^{-1}T^{-1}$$

$$(c) \quad \frac{[v^2]}{[t]} = \frac{(L/T)^2}{T} = \frac{L^2/T^2}{T} = \frac{L^2}{T^3}$$

$$(d) \quad \frac{[v^2]}{[x]} = \frac{(L/T)^2}{L} = \frac{L^2/T^2}{L} = \frac{L}{T^2}$$

Since acceleration has units of length divided by time squared, it is seen that the relation given in answer (d) is consistent with an expression yielding a value for acceleration.

10. The number of gallons of gasoline she can purchase is

$$\# \text{ gallons} = \frac{\text{total expenditure}}{\text{cost per gallon}} \approx \frac{33 \text{ Euros}}{\left(1.5 \frac{\text{Euros}}{\text{£}}\right) \left(\frac{1 \text{ £}}{1 \text{ quart}}\right) \left(\frac{4 \text{ quarts}}{1 \text{ gal}}\right)} \approx 5 \text{ gal}$$

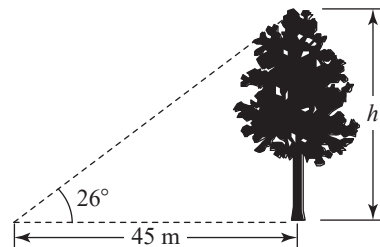
so the correct answer is (b).

11. The situation described is shown in the drawing at the right.

From this, observe that  $\tan 26^\circ = \frac{h}{45 \text{ m}}$ , or

$$h = (45 \text{ m}) \tan 26^\circ = 22 \text{ m}$$

Thus, the correct answer is (a).



12. Note that we may write  $1.365\,248\,0 \times 10^7$  as  $136.524\,80 \times 10^5$ . Thus, the raw answer, including the uncertainty, is  $x = (136.524\,80 \pm 2) \times 10^5$ . Since the final answer should contain all the digits we are sure of and one estimated digit, this result should be rounded and displayed as  $137 \times 10^5 = 1.37 \times 10^7$  (we are sure of the 1 and the 3, but have uncertainty about the 7). We see that this answer has three significant figures and choice (d) is correct.

## ANSWERS TO EVEN NUMBERED CONCEPTUAL QUESTIONS

2. Atomic clocks are based on the electromagnetic waves that atoms emit. Also, pulsars are highly regular astronomical clocks.

4. (a)  $\sim 0.5 \text{ lb} \approx 0.25 \text{ kg}$  or  $\sim 10^{-1} \text{ kg}$   
 (b)  $\sim 4 \text{ lb} \approx 2 \text{ kg}$  or  $\sim 10^0 \text{ kg}$   
 (c)  $\sim 4000 \text{ lb} \approx 2000 \text{ kg}$  or  $\sim 10^3 \text{ kg}$
6. Let us assume the atoms are solid spheres of diameter  $10^{-10} \text{ m}$ . Then, the volume of each atom is of the order of  $10^{-30} \text{ m}^3$ . (More precisely, volume =  $4\pi r^3/3 = \pi d^3/6$ .) Therefore, since  $1 \text{ cm}^3 = 10^{-6} \text{ m}^3$ , the number of atoms in the  $1 \text{ cm}^3$  solid is on the order of  $10^{-6}/10^{-30} = 10^{24}$  atoms. A more precise calculation would require knowledge of the density of the solid and the mass of each atom. However, our estimate agrees with the more precise calculation to within a factor of 10.
8. Realistically, the only lengths you might be able to verify are the length of a football field and the length of a housefly. The only time intervals subject to verification would be the length of a day and the time between normal heartbeats.
10. In the metric system, units differ by powers of ten, so it's very easy and accurate to convert from one unit to another.

### ANSWERS TO EVEN NUMBERED PROBLEMS

2. (a)  $L/T^2$  (b)  $L$
4. All three equations are dimensionally incorrect.
6. (a)  $\text{kg} \cdot \text{m}/\text{s}$  (b)  $Ft = p$
8. (a) 22.6 (b) 22.7 (c) 22.6 is more reliable
10. (a)  $3.00 \times 10^8 \text{ m/s}$  (b)  $2.9979 \times 10^8 \text{ m/s}$  (c)  $2.997925 \times 10^8 \text{ m/s}$
12. (a)  $346 \text{ m}^2 \pm 13 \text{ m}^2$  (b)  $66.0 \text{ m} \pm 1.3 \text{ m}$
14. (a) 797 (b) 1.1 (c) 17.66
16. 3.09 cm/s
18. (a)  $5.60 \times 10^2 \text{ km} = 5.60 \times 10^5 \text{ m} = 5.60 \times 10^7 \text{ cm}$   
 (b)  $0.4912 \text{ km} = 491.2 \text{ m} = 4.912 \times 10^4 \text{ cm}$   
 (c)  $6.192 \text{ km} = 6.192 \times 10^3 \text{ m} = 6.192 \times 10^5 \text{ cm}$   
 (d)  $2.499 \text{ km} = 2.499 \times 10^3 \text{ m} = 2.499 \times 10^5 \text{ cm}$
20. 10.6 km/L
22. 9.2 nm/s
24.  $2.9 \times 10^2 \text{ m}^3 = 2.9 \times 10^8 \text{ cm}^3$
26.  $2.57 \times 10^6 \text{ m}^3$

28.  $\sim 10^8$  steps30.  $\sim 10^8$  people with colds on any given day32. (a)  $4.2 \times 10^{-18} \text{ m}^3$  (b)  $\sim 10^{-1} \text{ m}^3$  (c)  $\sim 10^{16}$  cells34. (a)  $\sim 10^{29}$  prokaryotes (b)  $\sim 10^{14} \text{ kg}$ 

(c) The very large mass of prokaryotes implies they are important to the biosphere. They are responsible for fixing carbon, producing oxygen, and breaking up pollutants, among many other biological roles. Humans depend on them!

36. 2.2 m

38. 8.1 cm

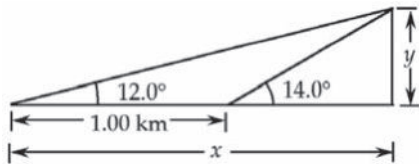
40.  $\Delta s = \sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos(\theta_1 - \theta_2)}$ 

42. 2.33 m

44. (a) 1.50 m (b) 2.60 m

46. 8.60 m

48. (a) and (b)



(c)  $y/x = \tan 12.0^\circ$ ,  $y/(x - 1.00 \text{ km}) = \tan 14.0^\circ$  (d)  $1.44 \times 10^3 \text{ m}$

50.  $y = \frac{d \cdot \tan \theta \cdot \tan \phi}{\tan \phi - \tan \theta}$ 

52. (a) 1.609 km/h (b) 88 km/h (c) 16 km/h

54. Assumes population of 300 million, average of 1 can/week per person, and 0.5 oz per can.

(a)  $\sim 10^{10}$  cans/yr (b)  $\sim 10^5$  tons/yr

56. (a)  $7.14 \times 10^{-2} \text{ gal/s}$  (b)  $2.70 \times 10^{-4} \text{ m}^3/\text{s}$  (c) 1.03 h58. (a)  $A_2/A_1 = 4$  (b)  $V_2/V_1 = 8$ 60. (a)  $\sim 10^2 \text{ yr}$  (b)  $\sim 10^4$  times62.  $\sim 10^4$  balls/yr. Assumes 1 lost ball per hitter, 10 hitters per inning, 9 innings per game, and 81 games per year.

## PROBLEM SOLUTIONS

- 1.1** Substituting dimensions into the given equation  $T = 2\pi\sqrt{\ell/g}$ , and recognizing that  $2\pi$  is a dimensionless constant, we have

$$[T] = \sqrt{\frac{[\ell]}{[g]}} \quad \text{or} \quad T = \sqrt{\frac{L}{L/T^2}} = \sqrt{T^2} = T$$

Thus, the dimensions are consistent.

- 1.2** (a) From  $x = Bt^2$ , we find that  $B = \frac{x}{t^2}$ . Thus,  $B$  has units of

$$[B] = \frac{[x]}{[t^2]} = \frac{L}{T^2}$$

- (b) If  $x = A \sin(2\pi ft)$ , then  $[A] = [x]/[\sin(2\pi ft)]$   
But the sine of an angle is a dimensionless ratio.

$$\text{Therefore, } [A] = [x] = \boxed{L}$$

- 1.3** (a) The units of volume, area, and height are:

$$[V] = L^3, [A] = L^2, \text{ and } [h] = L$$

We then observe that  $L^3 = L^2L$  or  $[V] = [A][h]$

Thus, the equation  $V = Ah$  is dimensionally correct.

- (b)  $V_{\text{cylinder}} = \pi R^2 h = (\pi R^2)h = Ah$ , where  $A = \pi R^2$

$$V_{\text{rectangular box}} = \ell wh = (\ell w)h = Ah, \text{ where } \boxed{A = \ell w = \text{length} \times \text{width}}$$

- 1.4** (a) In the equation  $\frac{1}{2}mv^2 = \frac{1}{2}mv_0^2 + \sqrt{mgh}$ ,  $[mv^2] = [mv_0^2] = M\left(\frac{L}{T}\right)^2 = \frac{ML^2}{T^2}$

while  $[\sqrt{mgh}] = \sqrt{M\left(\frac{L}{T^2}\right)L} = \frac{M^{\frac{1}{2}}L}{T}$ . Thus, the equation is dimensionally incorrect.

- (b) In  $v = v_0 + at^2$ ,  $[v] = [v_0] = \frac{L}{T}$  but  $[at^2] = [a][t^2] = \left(\frac{L}{T^2}\right)(T^2) = L$ . Hence, this equation is dimensionally incorrect.

- (c) In the equation  $ma = v^2$ , we see that  $[ma] = [m][a] = M\left(\frac{L}{T^2}\right) = \frac{ML}{T^2}$ , while  $[v^2] = \left(\frac{L}{T}\right)^2 = \frac{L^2}{T^2}$ .

Therefore, this equation is also dimensionally incorrect.

- 1.5** From the universal gravitation law, the constant  $G$  is  $G = Fr^2/Mm$ . Its units are then

$$[G] = \frac{[F][r^2]}{[M][m]} = \frac{(\text{kg} \cdot \text{m}/\text{s}^2)(\text{m}^2)}{\text{kg} \cdot \text{kg}} = \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2}$$

- 1.6 (a) Solving  $KE = \frac{p^2}{2m}$  for the momentum,  $p$ , gives  $p = \sqrt{2m(KE)}$  where the numeral 2 is a dimensionless constant. Dimensional analysis gives the units of momentum as:

$$[p] = \sqrt{[m][KE]} = \sqrt{M(M \cdot L^2/T^2)} = \sqrt{M^2 \cdot L^2/T^2} = M(L/T)$$

Therefore, in the SI system, the units of momentum are  $\boxed{\text{kg} \cdot (\text{m/s})}$ .

- (b) Note that the units of force are  $\text{kg} \cdot \text{m/s}^2$  or  $[F] = M \cdot L/T^2$ . Then, observe that

$$[F][t] = (M \cdot L/T^2) \cdot T = M(L/T) = [p]$$

From this, it follows that force multiplied by time is proportional to momentum:  $\boxed{Ft = p}$ . (See the impulse–momentum theorem in Chapter 6,  $F \cdot \Delta t = \Delta p$ , which says that a constant force  $F$  multiplied by a duration of time  $\Delta t$  equals the change in momentum,  $\Delta p$ .)

1.7  $Area = (length) \times (width) = (9.72 \text{ m})(5.3 \text{ m}) = \boxed{52 \text{ m}^2}$

- 1.8 (a) Computing  $(\sqrt{8})^3$  without rounding the intermediate result yields

$$(\sqrt{8})^3 = \boxed{22.6} \text{ to three significant figures.}$$

- (b) Rounding the intermediate result to three significant figures yields

$$\sqrt{8} = 2.8284 \rightarrow 2.83$$

Then, we obtain  $(\sqrt{8})^3 = (2.83)^3 = \boxed{22.7}$  to three significant figures.

- (c)  $\boxed{\text{The answer 22.6 is more reliable}}$  because rounding in part (b) was carried out too soon.

- 1.9 (a)  $78.9 \pm 0.2$  has  $\boxed{3 \text{ significant figures}}$  with the uncertainty in the tenths position.

- (b)  $3.788 \times 10^9$  has  $\boxed{4 \text{ significant figures}}$

- (c)  $2.46 \times 10^{-6}$  has  $\boxed{3 \text{ significant figures}}$

- (d)  $0.0032 = 3.2 \times 10^{-3}$  has  $\boxed{2 \text{ significant figures}}$ . The two zeros were originally included only to position the decimal.

1.10  $c = 2.997\,924\,58 \times 10^8 \text{ m/s}$

- (a) Rounded to 3 significant figures:  $c = \boxed{3.00 \times 10^8 \text{ m/s}}$

- (b) Rounded to 5 significant figures:  $c = \boxed{2.9979 \times 10^8 \text{ m/s}}$

- (c) Rounded to 7 significant figures:  $c = \boxed{2.997925 \times 10^8 \text{ m/s}}$

- 1.11 Observe that the length  $\ell = 5.62 \text{ cm}$ , the width  $w = 6.35 \text{ cm}$ , and the height  $h = 2.78 \text{ cm}$  all contain 3 significant figures. Thus, any product of these quantities should contain 3 significant figures.

(a)  $\ell w = (5.62 \text{ cm})(6.35 \text{ cm}) = \boxed{35.7 \text{ cm}^2}$

(b)  $V = (\ell w)h = (35.7 \text{ cm}^2)(2.78 \text{ cm}) = \boxed{99.2 \text{ cm}^3}$

$$(c) \quad wh = (6.35 \text{ cm})(2.78 \text{ cm}) = \boxed{17.7 \text{ cm}^2}$$

$$V = (wh)\ell = (17.7 \text{ cm}^2)(5.62 \text{ cm}) = \boxed{99.5 \text{ cm}^3}$$

- (d) In the rounding process, small amounts are either added to or subtracted from an answer to satisfy the rules of significant figures. For a given rounding, different small adjustments are made, introducing a certain amount of randomness in the last significant digit of the final answer.

$$1.12 \quad (a) \quad A = \pi r^2 = \pi(10.5 \text{ m} \pm 0.2 \text{ m})^2 = \pi[(10.5 \text{ m})^2 \pm 2(10.5 \text{ m})(0.2 \text{ m}) + (0.2 \text{ m})^2]$$

Recognize that the last term in the brackets is insignificant in comparison to the other two. Thus, we have

$$A = \pi[110 \text{ m}^2 \pm 4.2 \text{ m}^2] = \boxed{346 \text{ m}^2 \pm 13 \text{ m}^2}$$

$$(b) \quad C = 2\pi r = 2\pi(10.5 \text{ m} \pm 0.2 \text{ m}) = \boxed{66.0 \text{ m} \pm 1.3 \text{ m}}$$

- 1.13 The least accurate dimension of the box has two significant figures. Thus, the volume (product of the three dimensions) will contain only two significant figures.

$$V = \ell \cdot w \cdot h = (29 \text{ cm})(17.8 \text{ cm})(11.4 \text{ cm}) = \boxed{5.9 \times 10^3 \text{ cm}^3}$$

- 1.14 (a) The sum is rounded to  $\boxed{797}$  because 756 in the terms to be added has no positions beyond the decimal.

(b)  $0.0032 \times 356.3 = (3.2 \times 10^{-3}) \times 356.3 = 1.14016$  must be rounded to  $\boxed{1.1}$  because  $3.2 \times 10^{-3}$  has only two significant figures.

(c)  $5.620 \times \pi$  must be rounded to  $\boxed{17.66}$  because 5.620 has only four significant figures.

$$1.15 \quad d = (250\,000 \text{ mi}) \left( \frac{5\,280 \text{ ft}}{1.000 \text{ mi}} \right) \left( \frac{1 \text{ fathom}}{6 \text{ ft}} \right) = \boxed{2 \times 10^8 \text{ fathoms}}$$

The answer is limited to one significant figure because of the accuracy to which the conversion from fathoms to feet is given.

$$1.16 \quad v = \frac{\ell}{t} = \frac{186 \text{ furlongs}}{1 \text{ fortnight}} \left( \frac{1 \text{ fortnight}}{14 \text{ days}} \right) \left( \frac{1 \text{ day}}{8.64 \times 10^4 \text{ s}} \right) \left( \frac{220 \text{ yds}}{1 \text{ furlong}} \right) \left( \frac{3 \text{ ft}}{1 \text{ yd}} \right) \left( \frac{100 \text{ cm}}{3.281 \text{ ft}} \right)$$

giving  $v = \boxed{3.09 \text{ cm/s}}$

$$1.17 \quad 6.00 \text{ firkins} = 6.00 \text{ firkins} \left( \frac{9 \text{ gal}}{1 \text{ firkin}} \right) \left( \frac{3.786 \text{ L}}{1 \text{ gal}} \right) \left( \frac{10^3 \text{ cm}^3}{1 \text{ L}} \right) \left( \frac{1 \text{ m}^3}{10^6 \text{ cm}^3} \right) = \boxed{0.204 \text{ m}^3}$$

$$1.18 \quad (a) \quad \ell = (348 \text{ mi}) \left( \frac{1.609 \text{ km}}{1.000 \text{ mi}} \right) = \boxed{5.60 \times 10^2 \text{ km}} = \boxed{5.60 \times 10^5 \text{ m}} = \boxed{5.60 \times 10^7 \text{ cm}}$$

$$(b) \quad h = (1\,612 \text{ ft}) \left( \frac{1.609 \text{ km}}{5\,280 \text{ ft}} \right) = \boxed{0.4912 \text{ km}} = \boxed{491.2 \text{ m}} = \boxed{4.912 \times 10^4 \text{ cm}}$$

$$(c) \quad h = (20\,320 \text{ ft}) \left( \frac{1.609 \text{ km}}{5\,280 \text{ ft}} \right) = \boxed{6.192 \text{ km}} = \boxed{6.192 \times 10^3 \text{ m}} = \boxed{6.192 \times 10^5 \text{ cm}}$$

$$(d) \quad d = (8\,200 \text{ ft}) \left( \frac{1.609 \text{ km}}{5\,280 \text{ ft}} \right) = \boxed{2.499 \text{ km}} = \boxed{2.499 \times 10^3 \text{ m}} = \boxed{2.499 \times 10^5 \text{ cm}}$$

In (a), the answer is limited to three significant figures because of the accuracy of the original data value, 348 miles. In (b), (c), and (d), the answers are limited to four significant figures because of the accuracy to which the kilometers-to-feet conversion factor is given.

$$1.19 \quad v = 38.0 \frac{\cancel{\text{m}}}{\cancel{\text{s}}} \left( \frac{1 \cancel{\text{km}}}{10^3 \cancel{\text{m}}} \right) \left( \frac{1 \text{ mi}}{1.609 \cancel{\text{km}}} \right) \left( \frac{3\,600 \cancel{\text{s}}}{1 \text{ h}} \right) = 85.0 \text{ mi/h}$$

Yes, the driver is exceeding the speed limit by 10.0 mi/h.

$$1.20 \quad \text{efficiency} = 25.0 \frac{\cancel{\text{mi}}}{\cancel{\text{gal}}} \left( \frac{1 \text{ km}}{0.621 \cancel{\text{mi}}} \right) \left( \frac{1 \cancel{\text{gal}}}{3.786 \text{ L}} \right) = \boxed{10.6 \text{ km/L}}$$

$$1.21 \quad (a) \quad r = \frac{\text{diameter}}{2} = \frac{5.36 \text{ in}}{2} \left( \frac{2.54 \text{ cm}}{1 \text{ in}} \right) = \boxed{6.81 \text{ cm}}$$

$$(b) \quad A = 4\pi r^2 = 4\pi (6.81 \text{ cm})^2 = \boxed{5.83 \times 10^2 \text{ cm}^2}$$

$$(c) \quad V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi (6.81 \text{ cm})^3 = \boxed{1.32 \times 10^3 \text{ cm}^3}$$

$$1.22 \quad \text{rate} = \left( \frac{1}{32} \frac{\cancel{\text{in}}}{\cancel{\text{day}}} \right) \left( \frac{1 \cancel{\text{day}}}{24 \cancel{\text{h}}} \right) \left( \frac{1 \cancel{\text{h}}}{3\,600 \text{ s}} \right) \left( \frac{2.54 \cancel{\text{cm}}}{1.00 \cancel{\text{in}}} \right) \left( \frac{10^9 \text{ nm}}{10^2 \cancel{\text{cm}}} \right) = \boxed{9.2 \text{ nm/s}}$$

This means that the proteins are assembled at a rate of many layers of atoms each second!

$$1.23 \quad c = \left( 3.00 \times 10^8 \frac{\cancel{\text{m}}}{\cancel{\text{s}}} \right) \left( \frac{3\,600 \cancel{\text{s}}}{1 \text{ h}} \right) \left( \frac{1 \cancel{\text{km}}}{10^3 \cancel{\text{m}}} \right) \left( \frac{1 \text{ mi}}{1.609 \cancel{\text{km}}} \right) = \boxed{6.71 \times 10^8 \text{ mi/h}}$$

$$1.24 \quad \text{Volume of house} = (50.0 \text{ ft})(26 \text{ ft})(8.0 \text{ ft}) \left( \frac{2.832 \times 10^{-2} \text{ m}^3}{1 \text{ ft}^3} \right) \\ = \boxed{2.9 \times 10^2 \text{ m}^3} = (2.9 \times 10^2 \text{ m}^3) \left( \frac{100 \text{ cm}}{1 \text{ m}} \right)^3 = \boxed{2.9 \times 10^8 \text{ cm}^3}$$

$$1.25 \quad \text{Volume} = (25.0 \text{ acre} \cdot \cancel{\text{ft}}) \left( \frac{1 \text{ m}}{3.281 \cancel{\text{ft}}} \right) \left[ \left( \frac{43\,560 \cancel{\text{ft}^2}}{1 \text{ acre}} \right) \left( \frac{1 \text{ m}}{3.281 \cancel{\text{ft}}} \right)^2 \right] = \boxed{3.08 \times 10^4 \text{ m}^3}$$

$$1.26 \quad \text{Volume of pyramid} = \frac{1}{3}(\text{area of base})(\text{height}) \\ = \frac{1}{3}[(13.0 \text{ acres})(43\,560 \text{ ft}^2/\text{acre})](481 \text{ ft}) = 9.08 \times 10^7 \text{ ft}^3 \\ = (9.08 \times 10^7 \text{ ft}^3) \left( \frac{2.832 \times 10^{-2} \text{ m}^3}{1 \text{ ft}^3} \right) = \boxed{2.57 \times 10^6 \text{ m}^3}$$

1.27 Volume of cube =  $L^3 = 1$  quart (Where  $L$  = length of one side of the cube.)

$$\text{Thus, } L^3 = (1 \cancel{\text{quart}}) \left( \frac{1 \cancel{\text{gallon}}}{4 \cancel{\text{quarts}}} \right) \left( \frac{3.786 \cancel{\text{liter}}}{1 \cancel{\text{gallon}}} \right) \left( \frac{1000 \text{ cm}^3}{1 \cancel{\text{liter}}} \right) = 947 \text{ cm}^3$$

$$\text{and } L = \sqrt[3]{947 \text{ cm}^3} = \boxed{9.82 \text{ cm}}$$

- 1.28** We estimate that the length of a step for an average person is about 18 inches, or roughly 0.5 m.

Then, an estimate for the number of steps required to travel a distance equal to the circumference of the Earth would be

$$N = \frac{\text{Circumference}}{\text{Step Length}} = \frac{2\pi R_E}{\text{Step Length}} \approx \frac{2\pi(6.38 \times 10^6 \text{ m})}{0.5 \text{ m/step}} \approx 8 \times 10^7 \text{ steps}$$

or  $N \sim 10^8 \text{ steps}$

- 1.29.** We assume an average respiration rate of about 10 breaths/minute and a typical life span of 70 years. Then, an estimate of the number of breaths an average person would take in a lifetime is

$$n = \left(10 \frac{\text{breaths}}{\text{min}}\right) (70 \text{ yr}) \left(\frac{3.156 \times 10^7 \text{ s}}{1 \text{ yr}}\right) \left(\frac{1 \text{ min}}{60 \text{ s}}\right) = 4 \times 10^8 \text{ breaths}$$

or  $n \sim 10^8 \text{ breaths}$

- 1.30** We assume that the average person catches a cold twice a year and is sick an average of 7 days (or 1 week) each time. Thus, on average, each person is sick for 2 weeks out of each year (52 weeks). The probability that a particular person will be sick at any given time equals the percentage of time that person is sick, or

$$\text{probability of sickness} = \frac{2 \text{ weeks}}{52 \text{ weeks}} = \frac{1}{26}$$

The population of the Earth is approximately 7 billion. The number of people expected to have a cold on any given day is then

$$\text{Number sick} = (\text{population})(\text{probability of sickness}) = (7 \times 10^9) \left(\frac{1}{26}\right) = 3 \times 10^8 \text{ or } \sim 10^8$$

- 1.31** (a) Assume that a typical intestinal tract has a length of about 7 m and average diameter of 4 cm. The estimated total intestinal volume is then

$$V_{\text{total}} = A\ell = \left(\frac{\pi d^2}{4}\right)\ell = \frac{\pi(0.04 \text{ m})^2}{4}(7 \text{ m}) = 0.009 \text{ m}^3$$

The approximate volume occupied by a single bacterium is

$$V_{\text{bacteria}} \sim (\text{typical length scale})^3 = (10^{-6} \text{ m})^3 = 10^{-18} \text{ m}^3$$

If it is assumed that bacteria occupy one hundredth of the total intestinal volume, the estimate of the number of microorganisms in the human intestinal tract is

$$n = \frac{V_{\text{total}}/100}{V_{\text{bacteria}}} = \frac{(0.009 \text{ m}^3)/100}{10^{-18} \text{ m}^3} = 9 \times 10^{13} \text{ or } n \sim 10^{14}$$

- (b) The large value of the number of bacteria estimated to exist in the intestinal tract means that they are probably not dangerous. Intestinal bacteria help digest food and provide important nutrients. Humans and bacteria enjoy a mutually beneficial symbiotic relationship.

- 1.32** (a)  $V_{\text{cell}} = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi(1.0 \times 10^{-6} \text{ m})^3 = 4.2 \times 10^{-18} \text{ m}^3$

- (b) Consider your body to be a cylinder having a radius of about 6 inches (or 0.15 m) and a height of about 1.5 meters. Then, its volume is

$$V_{\text{body}} = Ah = (\pi r^2)h = \pi(0.15 \text{ m})^2(1.5 \text{ m}) = 0.11 \text{ m}^3 \text{ or } \sim 10^{-1} \text{ m}^3$$